

## Group - C

Answer any *one* of the following questions :

10×1=10

8. A particle in the harmonic oscillator potential starts out in the state :

$$\psi(x, 0) = A[3\psi_0(x) + 4\psi_1(x)]$$

- (a) Find A. 1
- (b) Construct  $\psi(x, t)$ . 1
- (c) What is the frequency of oscillation of  $|\psi(x, t)|^2$ ? 2
- (d) How the answer of "c" will change if  $\psi(x, 0) = A[3\psi_0(x) + 4\psi_2(x)]$ ? 4
- (e) What will be the average energy of the system in both the cases? 2
9. What is Larmor precession? Explain the theory of Anomalous Zeeman Effect. Why Paschen Back effect and Normal Zeeman effect have certain similarity? 3+5+2

2022

## 5th Semester Examination

## PHYSICS (Honours)

## [Quantum Mechanics and Applications]

Paper : C 11-T

[CBCS]

Full Marks : 40

Time : Two Hours

*The figures in the margin indicate full marks.  
Candidates are required to give their answers  
in their own words as far as practicable.*

## Group - A

1. Answer any *five* of the following questions : 2×5=10
- (a) Show that the momentum operator is Hermitian. 2
- (b) Which one of the following wave functions is a well-behaved wave function in the range  $-\infty < x < \infty$ ? Justify your answer.
- (i)  $\psi_1 = A \exp(-x)$
- (ii)  $\psi_2 = A \exp(-x^2)$
- (c) The operator  $\left(x + \frac{d}{dx}\right)$  has the eigenvalue  $\alpha$ .  
Derive the corresponding eigenfunction.

P.T.O.

( 2 )

- (d) In case of a quantum harmonic oscillator, show that zero-point energy is equal to  $(1/2) \hbar\omega$  using Heisenberg's uncertainty principle. 2
- (e) Plot the ground state and the first excited state wave functions of a linear harmonic oscillator. Also plot the corresponding probability density functions.
- (f) Two particles (masses  $m_1$  and  $m_2$ ) are attached to the ends of a massless rigid rod of length "a". The system is free to rotate in three dimensions about the (fixed) center of mass. Find out the allowed energy levels. 2
- (g) In the Stern-Gerlach experiment why is it necessary to use a beam of neutral atoms and not ions?
- (h) What are the values of L, S, and J and the multiplicity of the level having spectral term  ${}^4P_{5/2}$ ?

**Group - B**

Answer any **four** from the following questions :

5×4=20

2. Set up the time-independent Schrödinger equation for the one-dimensional potential

$$V(x) = 0 \text{ for } 0 < x < L$$

=  $\infty$  elsewhere.

Write the appropriate boundary conditions. Obtain the energy eigenvalues and the corresponding eigenfunctions.

1+2+2

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3. Determine the position probability density and the probability current density for the Gaussian wave packet

$$\psi(x, 0) = A \exp\left(ikx - \frac{a^2 x^2}{2}\right) \quad 2+3$$

4. Suppose a spin  $1/2$  particle is in a state :  $\chi = \begin{pmatrix} 1+i \\ 2 \end{pmatrix}$ . What are the probabilities of getting  $\hbar/2$  and  $-\hbar/2$  if you measure  $S_x$  and  $S_z$ ? 5
5. What is the most probable value of "r" in the ground state of Hydrogen? (Ground state is given by  $R_{10}(r) = 2a^{-3/2} \exp(-r/a)$ ) What are the sources of l-degeneracy and m-degeneracy. 3+2
6. (a) Show that the quantum mechanical probability of finding the linear harmonic oscillator in the ground state outside the classical limits of motion, is approximately 16%. (Given,  $\int_0^1 e^{-z^2} dz \approx 0.746$ )
- (b) What new information do we get from the quantum picture of a harmonic oscillator compared with the classical picture?
7. (a) Explain the origin of sodium D1 and D2 lines.
- (b) Show that  $[\hat{x}^3, p] = i\hbar 3\hat{x}^2$ . 3+2